

Algebra II

8-6

Some Useful Theorems

Theorem -

How many solutions do each of the following have?

$$P(x) = x^3 + 5x^2 - 7x + 1$$

$$P(x) = x^{12} - 3x^4 + 8x$$

$$P(x) = 4 + 3x^5 - 7x^6 + 11x^9 - 131x^2$$

Conjugate Root Theorem -

All but one of the equations solutions are given. Find the remaining root. (pg 380)

$$5) \quad x^3 - 3x^2 + 4x - 12 \quad \{ 3, 2i, \quad \}$$

Find a cubic equation with integral coefficients that has the given roots.

$$1) \quad \{ -1, 5i, \quad \}$$

A root of the equation is given. Solve the equation.

$$9) \quad x^3 + x - 10 = 0 \quad \{ -1+2i, \quad \}$$

Descartes' Rule of Signs -

$$*1) 3x^5 - 4x^3 - 7x^2 + 11x + 9 = 0$$

$$*2) 6x^6 + 7x^5 - x^4 + 2x^2 - x - 1 = 0$$

List all the possibilities for the nature of the roots of each equation.

$$13) x^4 + 3x^2 - 4 = 0$$

$$19) x^5 - x^3 - x^2 + x - 2 = 0$$

Assignment: pg 380 1-24 all
